

# Semi-empiirinen mallinnusmenetelmä merenpinnan nousun tutkimuksessa

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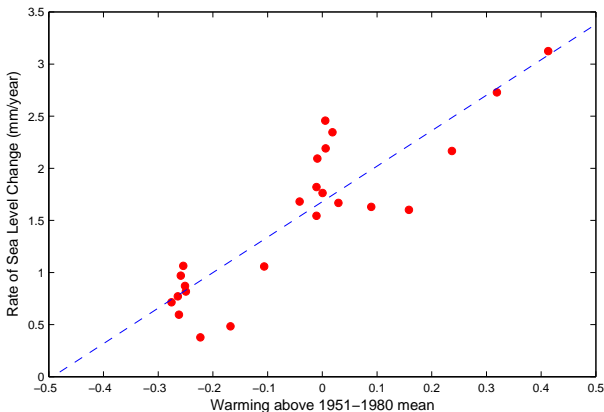








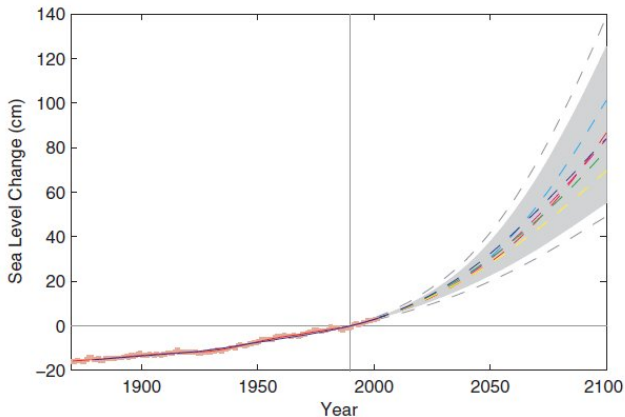
# $dH/dt$ against $T - T_0$ (Rahmstorf 2007)



Stefan Rahmstorf, June 2009  
Photo *Feature magazine*

# Projections to 2100 AD

based on IPCC Third Assessment Report [IPCC01] temperature scenarios.



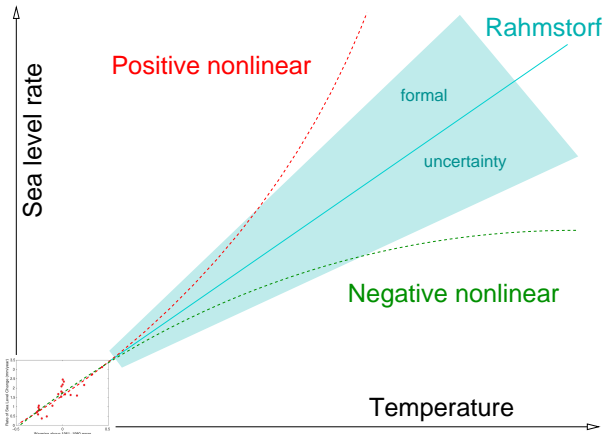
## Puoli-empiirinen mallinnus (2)

Called **semi**-empirical, as relationship conjectured is based in physics. Relationship derived from instrumental-period tide gauge and global mean temperature data is then extrapolated into 21st Century. Studies using general circulation model output provide further insight.

**Weakness:** we are **extrapolating**. The relationship is derived for a temperature range from 0.2-0.9K above pre-industrial, but applied for a range up to 6.5K above pre-industrial. . . seven times as much. E.g., non-linear ice sheet response could render fit inapplicable – see below.

Physical modelling doesn't have this problem in principle – but much harder in practice to do right.

# Limitation: we are *extrapolating!*



Vermeer & Rahmstorf, 2009, *Proceedings Nat. Acad. Sci.*

- ▶ Rahmstorf (2007) model [Rah07]:

$$\frac{dH}{dt} = a(T - T_0),$$

with  $T_0$  and  $a$  fit parameters. The  $a$  parameter describes the long-term response of both deep ocean and ice sheets to a temperature anomaly, cf. the “degree-day” rule of glaciology.

- ▶ New, **dual model** [VR09]

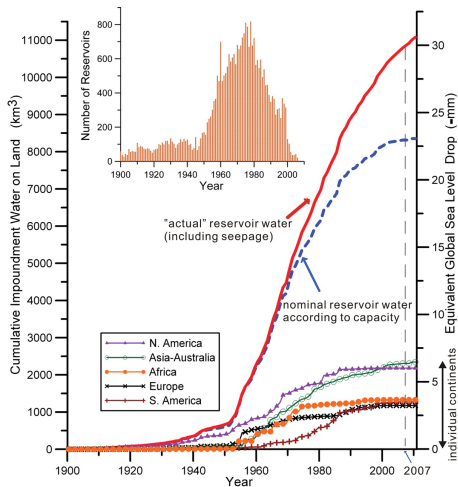
<http://www.pnas.org/content/106/51/21527.full.pdf>:

$$\frac{dH}{dt} = a(T - T_0) + b \frac{dT}{dt},$$

with a rapid response term and coefficient  $b$  added. Represents effects like the thermal expansion of ocean surface water, running to completion in a small number of years:  $\frac{dH}{dt} \sim \frac{dT}{dt} \Rightarrow H \sim T$ .

For fit to instrumental data, we obtain, surprisingly, a **negative**  $b$ .  
Interpretation: **delay**?

# Artificial reservoir effect

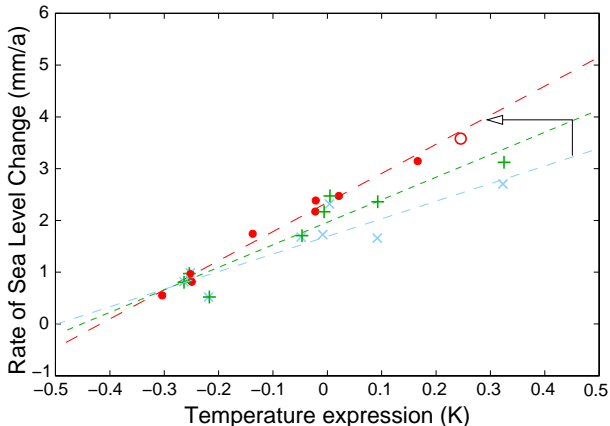


Chao *et al.* [CWL08] painstakingly tabulated the amount of water stored on land in artificial reservoirs. We use their curve, approximated by

$$\Delta H = 1.65 \text{ cm} + \frac{3.7 \text{ cm}}{\pi} \arctan \frac{t - 1978}{13},$$

to correct our sea level time series from [CW06].

## Dual model fit, stepwise improvement:



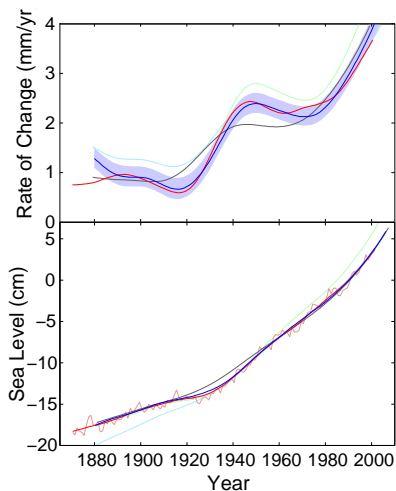
Blue: original  
Rahmstorf model

Green: after applying  
Chao *et al.*

Red: after  
introducing  $b$

Open circle:  
satellite altimetry  
(thx A. Cazenave)

... in the time domain:



Red: sea level data

Grey: original model fit

Blue: dual model fit

Light green, cyan: fits to  
the first half and second  
half of the data, respectively  
(cross-validation)

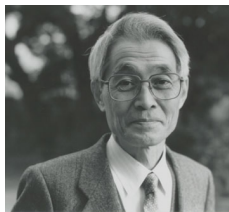
# Comparing the two models: are we 'fitting an elephant'?

Q. Is dual model fit significantly better?

A. Use Akaike Information Criterion (AIC<sub>c</sub>, [Aka74, BA02])

	Original model ( <i>a</i> only)	Dual model ( <i>a</i> and <i>b</i> )
<i>K</i>	4	5
RSS (cm <sup>2</sup> )	1.053	0.098
AIC <sub>c</sub>	5.11	4.75
Parameters	<i>a</i> , <i>T</i> <sub>0</sub> , <i>H</i> ( <i>t</i> <sub>0</sub> ), σ <sup>2</sup>	<i>a</i> , <i>b</i> , <i>T</i> <sub>0</sub> , <i>H</i> ( <i>t</i> <sub>0</sub> ), σ <sup>2</sup>

⇒ Dual model is “better”, even considering extra parameter and fewer degrees of freedom.



Hirotugu Akaike 1927-2009

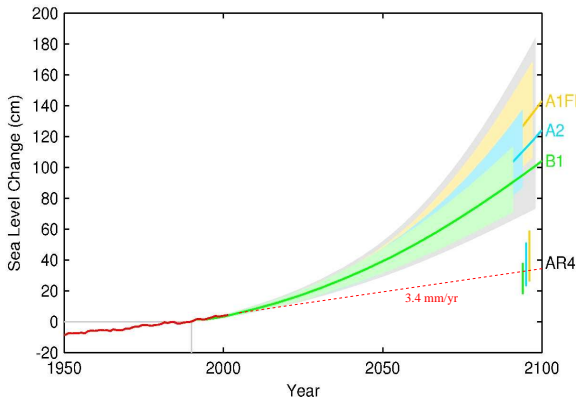
$$AIC_C = 2K + n \ln \frac{RSS}{n} + \frac{2K(K+1)}{n-K-1},$$

*n* number of data points (8)

*K* number of fit parameters including error variance σ<sup>2</sup>

*H*(*t*<sub>0</sub>) sea level integration constant.

# Dual model for 2100, and lessons



- ▶ Based on IPCC Fourth Assessment Report [IPCC07]
- ▶ Higher still (but **extrapolation** problem hasn't gone away!)
- ▶ Greatest inference uncertainty: emissions  $\Rightarrow$  temperatures, not temperatures  $\Rightarrow$  sea level
- ▶ Cuts needed to bring 2100AD sea level down must come **early**.

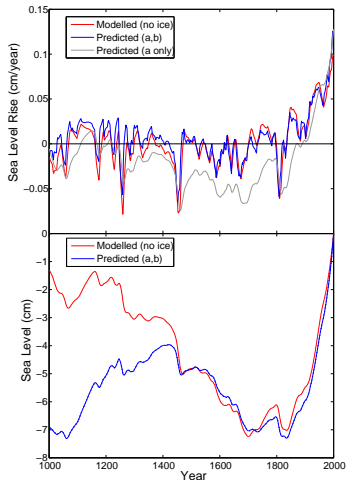
# The millennium run (1)

120 years, or eight 15-year bins, of instrumental data is very little. We don't have a thousand years of precise instrumental data, but we can *simulate* it – for **both** sea level and global mean temperature – using a **general circulation model** (GCM). We did so using the model CLIMBER-3 $\alpha$  [MGL<sup>+</sup>05].

- ▶ Does not model **land ice processes**
- ▶ However, in many ways physically realistic, containing the effects of Solar variability, volcanic eruptions, greenhouse gases and tropospheric aerosols
- ▶ Also two other models were tested: ECHO-G [vSZGR08] and ECBilt-CLIO [GRTB05].
- ▶ Variance explained 65-80%; better if (unrealistically) volcanic forcing “lumped” over latitude zones.

## The millennium run (2)

- ▶ Generated using the parameters fitted to a 1880-2000 simulation run.
- ▶ 15-year SSA smoothed
- ▶ **Red**: model output for sea level
- ▶ **Grey**: predicted using the  $a$ -only model
- ▶ **Blue**: predicted using the dual ( $a, b$ ) model. Note better capture of volcanic features
- ▶ Top:  $\frac{dH}{dt}$ , bottom:  $H$ .
- ▶ Small offset to  $T_0$  applied to eliminate drift 1500-1900; < 1400 needs different offset.



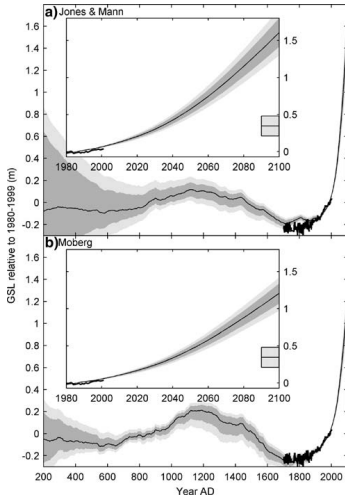
## Grinsted et al. (2009)

Interesting study: Grinsted *et al.* (2009) [GMJ09], who found on millennial time scale a sea level response component to temperature with time scale of a few hundred (up to a thousand) years.

Grinsted *et al.* used in addition to the instrumental record, two proxy reconstructions, those of [MSH<sup>+</sup>05], and of [JM04]. Additionally, they used the very long sea level record of Amsterdam for calibration.

Several other loose constraints were imposed.

# Results



The Grinsted *et al.* model is

$$H_{eq}(T) = aT(t) + b,$$

$$\tau \frac{dH(t)}{dt} = -(H(t) - H_{eq}(T)),$$

where  $H_{eq}$  is an “equilibrium sea level” at which ocean volume is assumed to remain constant. Real sea level  $H$  slowly tracks  $H_{eq}$  with a delay, or decay, time scale  $\tau$ .

# Upcoming paleo study

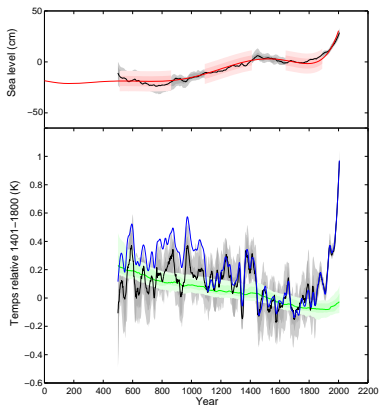
We have in preparation a study which replicates and improves on [GMJ09]. It uses as data:

- ▶ Mann *et al.* (2008) [MZH<sup>+</sup>08] for temperatures
- ▶ Superior quality sea level reconstructions by Kemp and Horton for the past two millennia from salt marsh proxies on the U.S. East Coast, e.g., [HPC<sup>+</sup>09].

The technique used by us was similar: Monte Carlo simulation of Bayesian inference. Temperature was inverted to a sea level prior using a variant of the Grinsted model, but with a non-zero “background” sea level rise. The posterior was obtained by fit to the sea level proxy data from salt marshes.

We use an equilibrium temperature  $T_0(t)$  rather than equilibrium sea level  $H_{eq}(T)$ .

## Results (1)



**Top:** A *posteriori* sea level curve (black/grey). Sea level proxy data represented by a polynomial fit, cutaway view (red/pink).

**Bottom:** Temperature curve from [MZH<sup>+</sup>08] (blue). A *posteriori* temperature curve (black/grey). Equilibrium temperature  $T_0(t)$  (green).

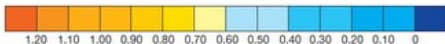
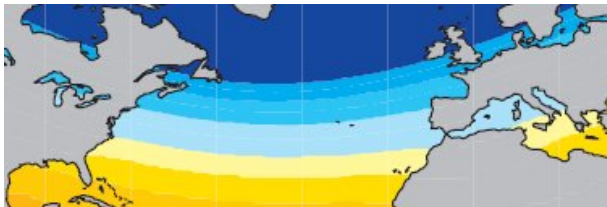
Uncertainty bands  $1\sigma$  and  $2\sigma$ .

## Results (2)

- ▶ We find an optimal  $\tau$  value of  $\sim 400$  years but with rather much uncertainty: 200-1000 years. Our results are **not** compatible with  $\tau = \infty$
- ▶ The background sea level rise rate (“infinite” time scale) is **small**, 0-0.2 mm/yr, best estimate 0.07 mm/yr [this is relative to a “no melt” rate, which is -0.3 mm/yr, Peltier]
- ▶ For the 20th and 21st Centuries, model reduces to earlier (dual) one – a design constraint
- ▶ For the time before AD 1100, it appears [MZH<sup>+</sup>08] is slightly high by 0.2K
- ▶ Work done by: Andrew Kemp, Ben Horton, Jeff Donnelly, Stefan Rahmstorf, Michael E. Mann and yours truly.

# Greenland fingerprint

Sea level rise is far from uniform!



When using proxy sea level data, one should consider, besides the correction for glacial isostatic adjustment after the last ice age, also the **fingerprint** of the various continental ice sheets.

Left: Greenland, Mitrovica *et al.* 2001 [MTDM01].

# Jälkikirjoitus:

## Siddall *et al.* 2009 (1)

- ▶ Heinäkuussa 2009 ilmestyi seuraava artikkeli:
  - ▶ Mark Siddall, Thomas F. Stocker & Peter U. Clark:  
“Constraints on future sea-level rise from past sea-level change”, *Nature Geoscience* 2, 571 - 575 (2009)
- ▶ Käytti semi-empiiristä menetelmää merenpinnan nousun ennustamiseksi vuoteen 2100 käyttäen merenpinnan ja globaalisen lämpötilan aineistoja viime jääkaudesta saakka
- ▶ Yllättävä tulos: nousu vain 7 – 82 cm, verrattavissa IPCC:n neljännen raportin 18-76 cm:n kanssa, mutta **paljon pienempi** kuin muut semi-empiiriset arviot!

## Siddall *et al.* 2009 (2)

- ▶ Kirjeenvaihto Rahmstorf-Vermeer ja tekijöiden välillä: laskennoista löytyi erehdyksiä
- ▶ Helmikuun 21. päivänä 2010 artikkeli **vedettiin takaisin**.
- ▶ Tieteellisen tuloksen **takaisin vetäminen** on tieteellisen prosessin osana, vaikkakin harvinaista:
- ▶ *Rehellinen virhe*, ja rehtiyden merkki. Missään vaiheessa **ei** ollut puhe tieteellisestä vilpistä!
- ▶ Virhe löytyi tutkijakollegojen, **ei** ilmastotieteen 'tilintarkastajien' toimesta.
- ▶ Ilmastopetkuttajat *eivät koskaan* vedä roska-artikkelinsa takaisin, ks. esim. **Ben Santerin avoin kirje**.

# Hullu Internet (1)

- ▶ Google: 'Siddall retraction' antaa 3 530 tulosta (26. helmikuuta)
- ▶ Guardian: *Climate scientists withdraw journal claims of rising sea levels*
- ▶ Climate Depot (Marc 'Swiftboat' Morano):



Oh No, Not Again! Scientists forced to retract study on sea level rise due to global warming

Sea Level Expert: Sea is not rising

- ▶ Vain muutama oikea maininta, esim. Wonk Room (vasemmistolainen):  
*Scientists Withdraw Journal Claims Of Limit To Rising Sea Levels.*

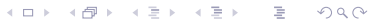


Kiitos kiinnostuksesta!



Kysymyksiä?

Photo: Liisa Vermeer





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